

Q1-1: Given that you are using K-means clustering algorithm to obtain 3 clusters from 7 data points in 2-dim. In the first iteration, clusters C1, C2 and C3 are assigned data points as below.

C1:  $\{(2,2),(4,4),(6,6)\}$ , C2:  $\{(0,4),(4,0)\}$ , C3:  $\{(5,5),(9,9)\}$

What will be the cluster centroids at the start of second iteration?

1. C1: (4,4), C2: (2,2), C3: (7,7)
2. C1: (6,6), C2: (4,4), C3: (9,9)
3. C1: (2,2), C2: (0,0), C3: (5,5)
4. C1: (2,6), C2: (0,4), C3: (5,9)

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Q1-2: Consider the K-means algorithm with  $K = 3$ . After current iteration, we have 3 centers  $C1: (0,1)$ ,  $C2: (2,1)$ ,  $C3: (-1,2)$ .

Which cluster assignment is possible for the points  $A: (1,1)$  and  $B: (-1,1)$  respectively? Assume ties are broken arbitrarily.

- (i)  $C1, C1$
- (ii)  $C2, C3$
- (iii)  $C1, C3$

1. Only (i)
2. Only (ii) and (iii)
3. Only (i) and (iii)
4. All of them

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Squared Euclidean distance  
between A and centers: 1, 1, 5

For B: 1, 9, 1

So A can be assigned to  $C1$  and  $C2$ , B can be to  $C1$  and  $C3$

Q1-3: Given the following points in 1D:  $x_1 = -1$ ,  $x_2 = 0$ ,  $x_3 = 1$ ,  $x_4 = 8$ ,  $x_5 = 9$ ,  $x_6 = 10$ , what are the locations of cluster centers at convergence assuming  $K=2$ ? Assume we start with cluster centers  $c_1 = 2$  and  $c_2 = 8$ .

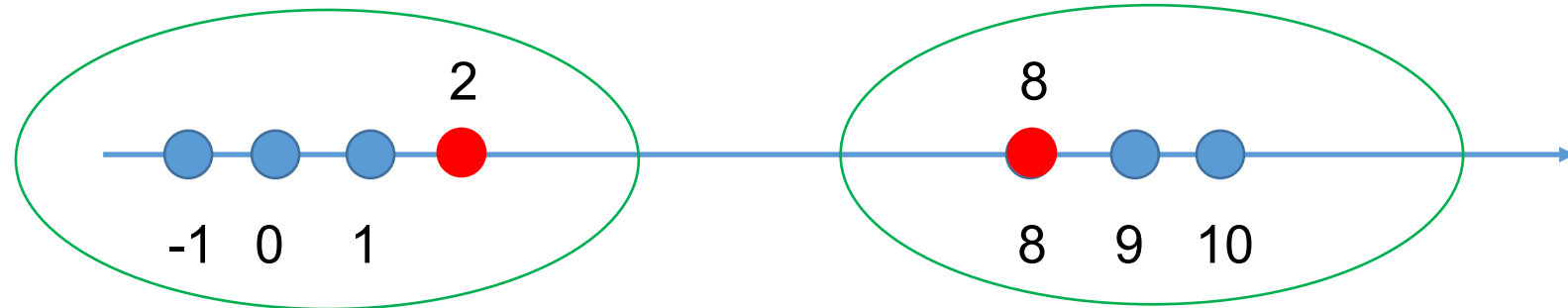
1.  $c_1 = 2, c_2 = 8$
2.  $c_1 = 0, c_2 = 9$
3.  $c_1 = -1, c_2 = 10$
4.  $c_1 = 0, c_2 = 0$



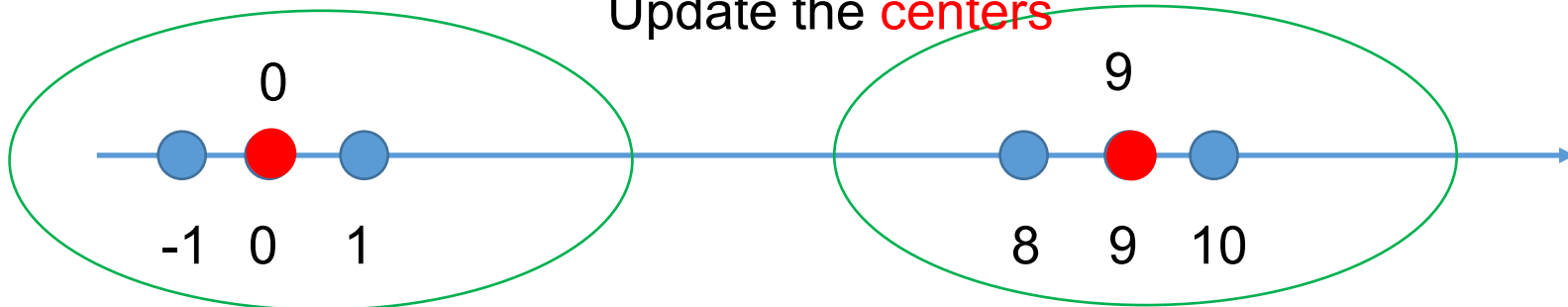
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1.  $c_1 = 2, c_2 = 8$
2.  $c_1 = 0, c_2 = 9$  ←
3.  $c_1 = -1, c_2 = 10$
4.  $c_1 = 0, c_2 = 0$

Assign the points to centers



Update the centers



Q2-1: Consider the K-means algorithm from the slides. Which step changes cluster centers to minimize distortion?

1. Step 1
2. Step 2

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Q2-2: Consider the K-means algorithm from the slides. Which step assigns each  $x$  to its closest cluster center  $y(x)$  to minimize the distortion?

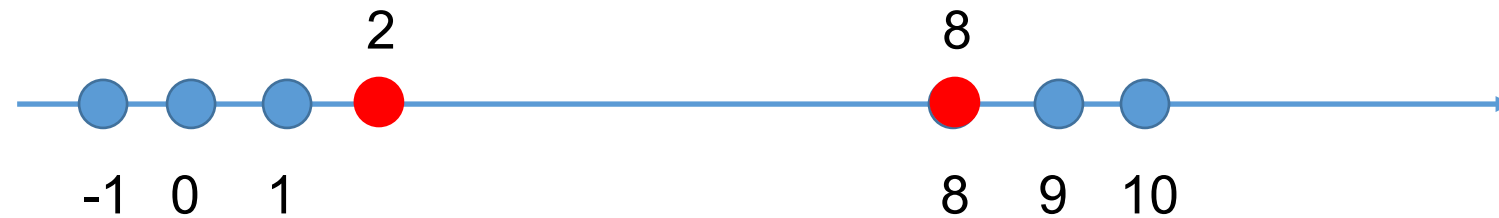
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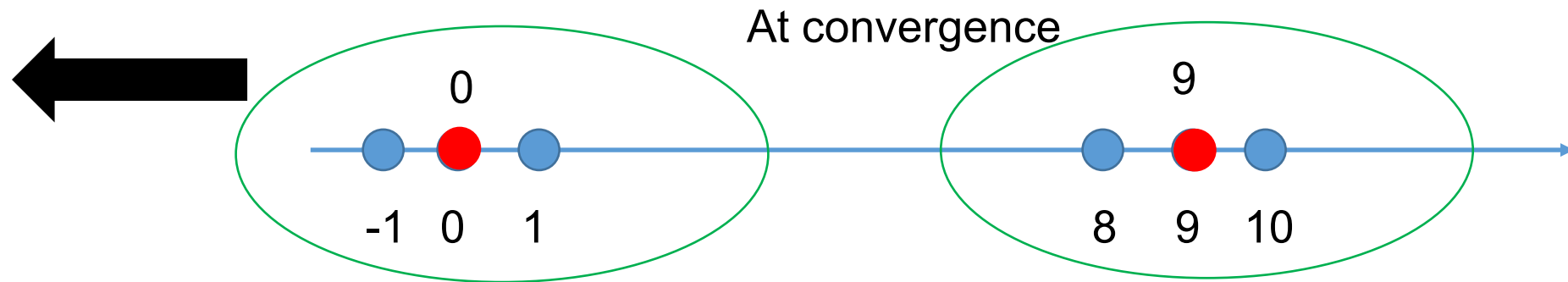
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1. 1, 0
2. 2, 2
3. 1, 4
4. 2, 4



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2. 2, 2
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4. 2, 4



Q2-4: If we choose number of clusters equal to number of data points, i.e.  $K = n$ , what will be the distortion of the dataset at convergence? Assume the starting cluster centers are same as the data points.

1. 0
2.  $n$
3. 1
4.  $n-1$

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1. 0 
2.  $n$
3. 1
4.  $n-1$

Q3-1: If we run K-means clustering twice with random starting cluster centers, are we guaranteed to get same clustering results?

1. Yes
2. No

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Q3-2: Is it guaranteed that K-means will always terminate? Does K-means always lead to global optimum?

1. Yes, Yes
2. No, Yes
3. Yes, No
4. No, No

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2. No, Yes

3. Yes, No



4. No, No

Q3-3: Which of the following could help for K-means to find a global optimum?

- i) Run K-means only for a fixed number of iterations
- ii) Run K-means multiple times with different starting cluster centers.
- iii) Pick the starting cluster centers intelligently.

1. only (i)
2. (i) and (ii)
3. (i) and (iii)
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4. (ii) and (iii)

